

# Contents

**Preface** ix

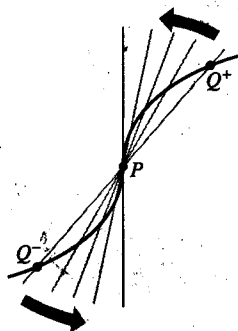
**Prologue** xv

## **Chapter 1** **The Rate of Change of a** **Function**

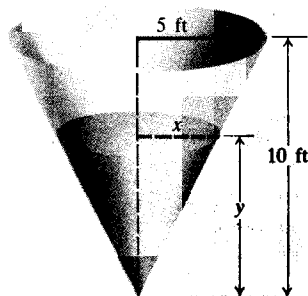
- 1.1** Cartesian Coordinates and Equations for Lines 1
  - 1.2** Functions and Their Graphs 12
  - 1.3** Calculus and Computation 24
  - 1.4** Absolute Value (Magnitude) and Target Values 31
  - 1.5** Shifts, Circles, and Parabolas 39
  - 1.6** Slopes, Tangent Lines, and Derivatives 48
  - 1.7** Limits of Function Values 58
  - 1.8** Limits Involving Infinity 73
  - 1.9** The Sandwich Theorem and  $(\sin \theta)/\theta$  79
  - 1.10** Continuous Functions 84
- Review Questions 94
- Miscellaneous Exercises 95

## **Chapter 2** **Derivatives**

- 2.1** Differentiation Rules 101
  - 2.2** Velocity and Other Rates of Change 113
  - 2.3** Derivatives of Trigonometric Functions 125
  - 2.4** The Chain Rule 132
  - 2.5** Implicit Differentiation and Fractional Powers 141
  - 2.6** Linearization and Differentials 148
  - 2.7** Newton's Method 161
- Review Questions 170
- Miscellaneous Exercises 171



### Chapter 3 Applications of Derivatives

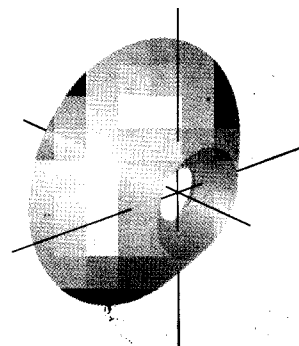


- 3.1** Related Rates of Change 177
- 3.2** Maxima, Minima, and the Mean Value Theorem 184
- 3.3** Graphing with  $y'$  and  $y''$  192
- 3.4** Graphing Rational Functions: Asymptotes and Dominant Terms 201
- 3.5** Optimization 207
- 3.6** Indeterminate Forms and L'Hôpital's Rule 220
- 3.7** Approximation Errors, Quadratic Approximations, and the Mean Value Theorem 226
- Review Questions 234
- Miscellaneous Exercises 234

### Chapter 4 Integration

- 4.1** Indefinite Integrals 239
- 4.2** Initial Value Problems and Mathematical Modeling 247
- 4.3** Definite Integrals 255
- 4.4** Evaluating Definite Integrals (First Steps) 269
- 4.5** The Fundamental Theorem of Integral Calculus 278
- 4.6** Integration by Substitution: Running the Chain Rule Backward 288
- 4.7** Numerical Integration 297
- Review Questions 311
- Miscellaneous Exercises 311

### Chapter 5 Applications of Definite Integrals

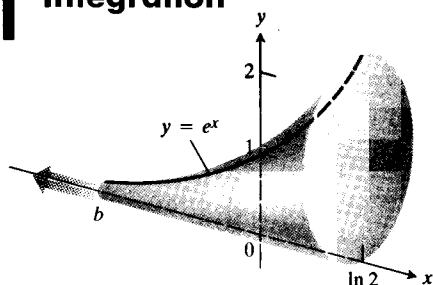


- 5.1** Areas of Regions Between Curves 317
- 5.2** Volumes: Slicing, Disks, and Washers 324
- 5.3** Cylindrical Shells: An Alternative to Washers 338
- 5.4** Lengths of Curves in the Plane 346
- 5.5** Areas of Surfaces of Revolution 352
- 5.6** Moments and Centers of Mass 359
- 5.7** Work 369
- 5.8** Fluid Pressures and Fluid Forces 378
- 5.9** The Basic Pattern: Other Modeling Applications 384
- Review Questions 393
- Miscellaneous Exercises 393

## Chapter 6 The Calculus of Transcendental Functions

- 6.1** Inverse Functions 397
- 6.2** Natural Logarithms 402
- 6.3** The Exponential Function 412
- 6.4** Other Exponential and Logarithmic Functions 421
- 6.5** Growth and Decay 431
- 6.6** The Rates at Which Functions Grow 440
- 6.7** The Inverse Trigonometric Functions 446
- 6.8** Derivatives of Inverse Trigonometric Functions; Related Integrals 452
- 6.9** Hyperbolic Functions 457
- 6.10** Hanging Cables 468
- Review Questions 474
- Miscellaneous Exercises 474

## Chapter 7 Techniques of Integration



- 7.1** Basic Integration Formulas 479
- 7.2** Integration by Parts 486
- 7.3** Trigonometric Integrals 493
- 7.4** Trigonometric Substitutions 501
- 7.5** Rational Functions and Partial Fractions 508
- 7.6** Using Integral Tables; Reduction Formulas 513
- 7.7** Improper Integrals 519
- Review Questions 531
- Miscellaneous Exercises 531

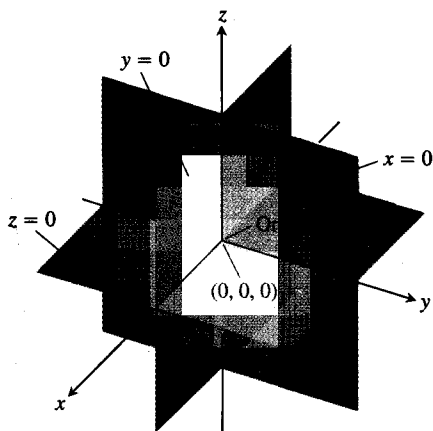
## Chapter 8 Infinite Series

- 8.1** Limits of Sequences of Numbers 537
- 8.2** Infinite Series 553
- 8.3** Series Without Negative Terms: The Comparison and Integral Tests 563
- 8.4** Series Without Negative Terms: The Ratio and Root Tests 572
- 8.5** Alternating Series and Absolute Convergence 578
- 8.6** Power Series 586
- 8.7** Taylor Series and Maclaurin Series 594
- 8.8** Calculations with Taylor Series 608
- 8.9** A Computer Mystery (Optional) 615
- Review Questions 617
- Miscellaneous Exercises 618

## Chapter 9 Conic Sections, Parametrized Curves, and Polar Coordinates

- 9.1** Equations for Conic Sections 623  
**9.2** The Graphs of Quadratic Equations in  $x$  and  $y$ ; Rotations About the Origin 640  
**9.3** Parametrizations of Curves 649  
**9.4** The Calculus of Parametrized Curves 658  
**9.5** Polar Coordinates 664  
**9.6** Graphing in Polar Coordinates 670  
**9.7** Polar Equations for Conic Sections 677  
**9.8** Integration in Polar Coordinates 683  
 Review Questions 691  
 Miscellaneous Exercises 691

## Chapter 10 Vectors and Analytic Geometry in Space

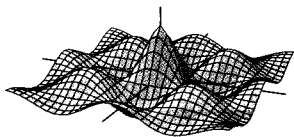


- 10.1** Vectors in the Plane 699  
**10.2** Cartesian (Rectangular) Coordinates and Vectors in Space 708  
**10.3** Dot Products 718  
**10.4** Cross Products 725  
**10.5** Lines and Planes in Space 731  
**10.6** Products of Three Vectors or More 741  
**10.7** Surfaces in Space 746  
**10.8** Cylindrical and Spherical Coordinates 758  
 Review Questions 762  
 Miscellaneous Exercises 762

## Chapter 11 Vector-Valued Functions and Motion in Space

- 11.1** Vector-Valued Functions and Space Curves 767  
**11.2** Modeling Projectile Motion 779  
**11.3** Directed Distance and the Unit Tangent Vector  $\mathbf{T}$  786  
**11.4** Curvature, Torsion, and the Frenet Frame 791  
**11.5** Planetary Motion and Satellites 802  
 Review Questions 810  
 Miscellaneous Exercises 811

## Chapter 12 Functions of Two or More Variables and Their Derivatives



$$z = (\cos x)(\cos y) e^{-\sqrt{x^2+y^2}/4}$$

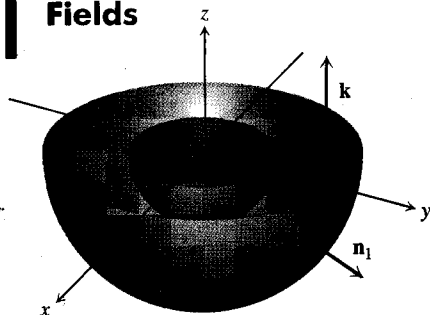
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- 12.1** Functions of Two or More Independent Variables 815
- 12.2** Limits and Continuity 825
- 12.3** Partial Derivatives 833
- 12.4** Differentiability, Linearization, and Differentials 842
- 12.5** The Chain Rule 854
- 12.6** Partial Derivatives with Constrained Variables 862
- 12.7** Directional Derivatives, Gradient Vectors, and Tangent Planes 869
- 12.8** Maxima, Minima, and Saddle Points 881
- 12.9** Lagrange Multipliers 891
- 12.10** Taylor's Formula, Second Derivatives, and Error Estimates 902
- Review Questions 908
- Miscellaneous Exercises 909

## Chapter 13 Multiple Integrals

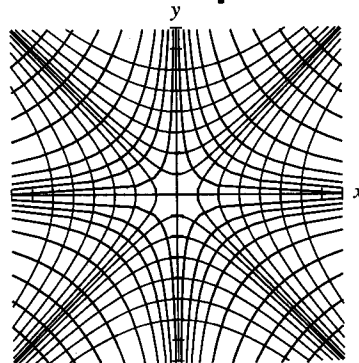
- 13.1** Double Integrals 915
- 13.2** Areas, Moments, and Centers of Mass 928
- 13.3** Double Integrals in Polar Form 937
- 13.4** Triple Integrals in Rectangular Coordinates: Volumes and Average Values 943
- 13.5** Masses and Moments in Three Dimensions 950
- 13.6** Triple Integrals in Cylindrical and Spherical Coordinates 955
- 13.7** Substitutions in Multiple Integrals 962
- Review Questions 969
- Miscellaneous Exercises 969

## Chapter 14 Integration in Vector Fields



- 14.1** Line Integrals 973
- 14.2** Vector Fields, Work, Circulation, and Flux 979
- 14.3** Green's Theorem in the Plane 988
- 14.4** Surface Area and Surface Integrals 1001
- 14.5** The Divergence Theorem 1013
- 14.6** Stokes's Theorem 1023
- 14.7** Path Independence, Potential Functions, and Conservative Fields 1030
- Review Questions 1040
- Miscellaneous Exercises 1041

## Chapter 15 Differential Equations



(Generated by Mathematica)

- 15.1** Separable First Order Equations 1045
- 15.2** Exact Differential Equations 1052
- 15.3** Linear First Order Equations 1055
- 15.4** Linear Homogeneous Second Order Equations 1061
- 15.5** Second Order Equations; Reduction of Order 1066
- 15.6** Oscillation 1080
- 15.7** Power Series Solutions 1084
- 15.8** Slope Fields and Picard's Theorem 1088
- 15.9** Numerical Methods 1093
- Review Questions 1099
- Miscellaneous Exercises 1099

## Appendices

- A.1** Formulas from Precalculus Mathematics A-1
- A.2** A Brief Review of Trigonometric Functions A-5
- A.3** Symmetry in the  $xy$ -Plane A-16
- A.4** Proofs of the Limit Theorems in Chapter 1 A-17
- A.5** Mathematical Induction A-21
- A.6** Complex Numbers A-24
- A.7** Cauchy's Mean Value Theorem and the Stronger Form of L'Hôpital's Rule A-25
- A.8** Limits That Arise Frequently A-26
- A.9** The Distributive Law for Vector Cross Products A-28
- A.10** Determinants and Cramer's Rule A-30
- A.11** Euler's Theorem and the Increment Theorem A-37
- A.12** Numerical Tables for  $\sin x$ ,  $\cos x$ ,  $\tan x$ ,  $e^x$ ,  $e^{-x}$ , and  $\ln x$  A-42
- A.13** Vector Operator Formulas in Cartesian, Cylindrical, and Spherical Coordinates; Vector Identities A-44

**Answers A-47**

**Index I-1**

**A Brief Table of Integrals T-1**